

Figure 19.2 Two strings stuck on a D2-brane.

Because the fundamental things of string theory are extended objects, string theory is intrinsically free of ultraviolet divergences. It provides a finite theory of quantum gravity.

19.7 Riemann Surfaces and Moduli

A homeomorphism is a map that is one to one and continuous with a continuous inverse. A **Riemann surface** is a two-dimensional real manifold whose open sets U_{α} are mapped onto open sets of the complex plane \mathbb{C} by homeomorphisms z_{α} whose transition functions $z_{\alpha} \circ z_{\beta}^{-1}$ are analytic on the images of the intersections $U_{\alpha} \cap U_{\beta}$. Two Riemann surfaces are **equivalent** if they are related by a continuous analytic map that is one to one and onto.

A parameter that distinguishes a Riemann surface from other, inequivalent Riemann surfaces is called a **modulus**. Some Riemann surfaces have